VALUING EMPLOYEE STOCK OPTIONS AND RESTRICTED STOCK IN THE PRESENCE OF MARKET IMPERFECTIONS

by

M Abudy S. Benninga

Working Paper No 17/2010

December 2010

Research No. 01700100

This paper was partially financed by the Henry Crown Institute of Business Research in Israel.

The Institute's working papers are intended for preliminary circulation of tentative research results. Comments are welcome and should be addressed directly to the authors.

The opinions and conclusions of the authors of this study do not necessarily state or reflect those of The Faculty of Management, Tel Aviv University, or the Henry Crown Institute of Business Research in Israel.

Valuing employee stock options and restricted stock in the presence of market imperfections^{*}

Menachem Abudy Bar Ilan University abudymen@post.tau.ac.il

Simon Benninga Tel Aviv University benninga@post.tau.ac.il

This version: December 30, 2010

ABSTRACT

We develop a new technology for valuing financial assets such as employee stock options and restricted stocks. Our model takes explicit account of the non-diversification of the owner of the asset. The model is an extension of the common binomial pricing model and is relatively easy to implement. This paper explains the issues and uses a database of employee stock options to estimate the model parameters.

^{*} We thank KPMG for a research grant. This paper is based on Abudy's dissertation at Tel Aviv University. Previous research has also benefited from a grant from the Israel Institute of Business Research at Tel Aviv University.

Valuing employee stock options and restricted stock in the presence of market imperfections

1. Introduction

In this paper we introduce a simple model for the valuation of employee stock options (ESO) that takes account of market imperfections. The model, based on a paper by Benninga, Helmantel, Sarig (2005, henceforth BHS) directly incorporates non-marketability into asset valuation and is easy to implement in a binomial framework. A simple extension of the model can also be used to value restricted stock units (RSU).

The extensive literature on employee stock options can be divided into three segments. Our model relates to all three of these segments.

Valuation of ESOs: A significant segment of the literature discusses the value of an employee stock option. The <u>arbitrage-pricing approach</u> of this literature (for example Hull-White 2004, Cvitanić et al. 2007) uses either lattice-based or continuous-time valuation frameworks to value the ESO with its special features. The <u>utility approach</u> of the valuation literature assumes that an employee has a utility function and uses utility-based models to value the ESO (for example Hull and Murphy 2002). Both the arbitrage approach and the utility approach to valuation tend to the conclusion that the Black-Scholes and binomial pricing models overvalue ESOs. However, while the arbitrage strand of the literature results in explicit pricing formulas of ESOs, the utility approach is not as explicit—pricing in this approach is a function of risk aversion and employee income and wealth.

Our model falls into the category of the arbitrage approach models. However, whereas the arbitrage-approach models cited above require somewhat arbitrary assumptions about early exercise, our model endogenizes this decision into the pricing function.

Documenting employee behavior: Another segment of the ESO literature documents actual behavior of the holders of employee stock options. Typically this strand of the literature documents the early-exercise behavior of ESO holders. Huddart and Lang (1996, 2003), Carpenter, Stanton and Wallace (2009) are typical exponents of this part of the literature.

The employee-behavior part of the ESO literature shows clearly that employees tend to earlyexercise their options. This behavior contradicts the prediction of standard option-pricing models, in which early exercise of calls is nearly always sub-optimal. Early exercise of ESOs has been attributed to various reasons, typically the difficulty of employees hedging or trading their ESOs, even when the vesting period has passed, because of the long-term nature of the ESO.

This paper is also part of the employee behavior strand of the ESO literature in two ways. First, analytical model explains early exercise of ESOs by pricing the non-diversifiable aspects of the ESO. Second, our large and unique data base of Israeli ESOs enables us to both document early-exercise and calibrate our model's non-diversifiability.

Accounting cost of ESOs: IFRS2 and FAS 123R require an attribution of cost to the grant of employee stock options. Abstracting from philosophical issues of cost versus value¹ the actual implementation of the accounting regulations typically ascribes the ESO cost using a standard valuation model, be it Black-Scholes or one of the other lattice models discussed above. Roughly speaking this literature (of which Chance 2004, Rubinstein 1995, and Hall and Murphy 2002 are the most important articles) discusses whether the accounting cost of an ESO should be its value in a perfect-markets setting or the value incorporating the various option restrictions. Our contribution to the accounting discussion is to provide an explicit pricing model that accounts for non-diversification and is both easily implementable and has some connection to the non-diversification of the ESO holder.

Another approach to this problem is due to Finnerty (2005). Finnerty describes a framework in which an investor buys the ESO rights from an employee. These rights are freely transferable, and the outside investor is fully diversified with respect to the risk associated with each ESO. The price of the ESO rights contract is negotiated between the employee and the investor therefore measures the value of the ESO to the employee. Our model has different perspective: We assume that the employee granted ESOs cannot achieve full diversification, and consider this explicitly in the pricing model.

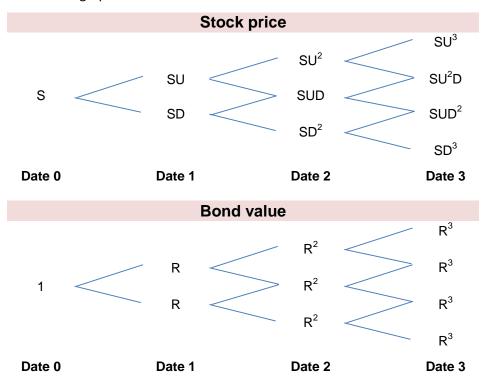
A further contribution of our model is to the pricing of restricted stock units. Current accounting regulations require that RSUs be priced at the market value of the stock on the grant date. Our model prices the RSUs and shows that their true economic value is far below the market value. We thus provide the basis for an "argument" with the IFRS and FASB.

¹ See Chance (2004) and Rubinstein (1995). We find this discussion too philosophical and abstract to be useful.

2. A review of the binomial model

The binomial model is, after the Black-Scholes model, the best-known option pricing model. In this section we review this model. The advantages of the binomial model are its simplicity, its easy computability, and (under appropriate assumptions) its congruence with the Black-Scholes framework.

Suppose we are trying to price an option on a stock. Suppose further that the option has exercise price X and that the current price of the stock is S. We divide the interval (0,T) into n subintervals of length Δt : $\{0, \Delta t, 2\Delta t, ..., n\Delta t = T\}$. The binomial model assumes that in each time period Δt the price of the underlying asset either goes up by a factor U or down by factor D. R (r) is the gross (net) risk free rate in the economy; if $U \ge R \ge D$ no-arbitrage opportunities exist in the market.² Thus at time Δt is the stock price is either *SU* or *SD*. By recursion, the price of the underlying asset at time j Δ is one of the following prices: $\{SU^{j}, SU^{j-1}D, SU^{j-2}D^{2}, ..., SD^{j}\}$.



The graphical version of this model is well-known:

² U, D, and R are related to the size of the interval Δt , but for simplicity we have repressed this relationship in our notation. For completeness: If U and D are derived from a lognormal process with annual mean μ and standard deviation σ , then $U = \exp\left[\mu\Delta + \sigma\sqrt{\Delta t}\right]$, $D = \exp\left[\mu\Delta - \sigma\sqrt{\Delta t}\right]$, and $R = \exp[r\Delta t]$.

State prices in a binomial model

At any time j Δ t there are two future states of the world, typified by the two possible stock prices SU^{j} or SD^{j} . The state price q_{U} is the per-dollar discount factor for dollars in the "Up" state (where the stock price is SU^{j}) and the state price q_{D} is the per-dollar discount factor for the other state. Graphically:



Notice that $q_u + q_d$ price an asset that pays off 1 in each of the future states. The financial meaning of this property is that the sum of the state prices prices a risk-free asset, (i.e., $\frac{1}{R} = q_U + q_D$, where R is the gross risk-free interest rate). It can be shown that $q_U = \frac{D-R}{R(U-D)}$, $q_U = \frac{U-R}{R(U-D)}$.

Given the state prices, we can easily price European or American options. For example, a European call and put on the stock with expiration T and strike X can be priced by:

$$Call = \sum_{i=0}^{n} {n \choose i} q_{U}^{i} q_{D}^{n-i} Max \left(SU^{i} D^{n-i} - X, 0 \right)$$
$$Put = \sum_{i=0}^{n} {n \choose i} q_{U}^{i} q_{D}^{n-i} Max \left(X - SU^{i} D^{n-i}, 0 \right)$$

American options can also be priced by using the state prices.³

3. Public versus private state prices

Our model is based on the assumption that state prices depend on whether an individual can freely dispose or buy the asset under question. If an individual operates in competitive markets, then the asset is priced by "public state prices" $q_U^{public} = \frac{R-D}{R(U-D)}$ and $q_D^{public} = \frac{U-R}{R(U-D)}$ as defined in

the previous section. If, however, the holder of the asset is restricted in selling the asset, we assume that a different set of state prices holds. We call these prices the "private state prices" and assume that

$$\begin{split} q_U^{private} &= q_U^{public} - \delta \\ q_D^{private} &= q_D^{public} + \delta \end{split}$$

³ See Benninga, *Financial Modeling*, 2008, Chapter 19 for details.

Why do private state prices differ from public prices?

In this section we offer an informal intuitive approach to the model.⁴ The easiest way to think about public versus private state prices is to consider a numerical example. Suppose that $\Delta t = 1$ (meaning that we consider annual payoffs and returns) and that $q_U^{public} = 0.3$, $q_D^{public} = 0.6$. This means that an asset paying 1 in the Up state and 0 in the Down state is valued at 0.3 today and that an asset paying 0 in the Up and 1 in the Down is valued at 0.6 today. It also means that the interest rate is 11.11%:

$$r = R - 1 = \frac{1}{q_U^{public} + q_D^{public}} - 1 = \frac{1}{0.9} - 1 = 11.11\%$$

Now suppose that, following our model, restricted assets are priced by private state prices. If δ = 0.02 then:

$$q_U^{private} = 0.3 - \delta = 0.28$$
$$q_D^{private} = 0.6 + \delta = 0.62$$

The private state prices indicate that assets that pay off in the Up state are worth less than if they were traded and assets that pay off in the Down state are worth more. This means that a call option is worth less in the "private market" than in the "public market."⁵

The intuition behind the private state prices is that an individual who holds restricted assets—be they stock or employee stock options—suffers from non-diversification, and that this non-diversification expresses itself in the individual having a more-than-optimal amount in Up states and less-than-optimal amount in Down states of the world. If the individual is nondiversified, she is more exposed to the underlying asset's volatility. Consider, for example, an employee in XYZ Corp. who has been given employee stock options in XYZ as part of her compensation package. Since the employee's wages are already tied to the fortunes of XYZ, the addition of (restricted) stock options further increases the employee's dependence on the company. If the employee were allowed to optimally diversify by selling the options, she would purchase assets that are negatively correlated with the fortunes of XYZ, paying off more if XYZ ended in a Down state of the world. The fact that she cannot diversify leads her to value Up-state payoffs less than the market and Down-state payoffs more than the market valuation.

⁴ For a formal model and derivation, see BHS (2005) and Abudy and Benninga (2010).

⁵ Of course there is no "private market," but we use this as convenient shorthand.

We express this non- diversification of the ESO holder by assuming that her private state prices value the Up state of the world less than the public state prices and that the private state prices value the Down state of the world more than the public state prices. This is what is meant by the conditions

 $q_U^{private} = q_U^{public} - \delta, \ q_D^{private} = q_D^{public} + \delta \,.$

The symmetry in δ means that $q_U^{private} + q_D^{private} = q_U^{public} + q_D^{public} = \frac{1}{R}$ and is meant to express the assumption that the non-diversified individual has the same access to borrowing/lending markets as the diversified individual.⁶

Private state prices lead to early call option exercise

A remarkable result of our public vs. private pricing model is that an individual who prices options using his private state prices will find it optimal to early-exercise a call option. To frame this result, recall that a standard result in option pricing theory is that the market price of call option on a non-dividend paying stock is always higher than the option's intrinsic value.⁷ If, however, the individual prices an option using private state prices, this result no longer holds, and there is always a point where the individual would prefer early exercise to continued holding of the option.

We have rigorously proved this assertion in another paper.⁸ In this section we will indicate the rough outlines of the proof and provide a graphical example. Recall from section 1 that a European call option on a stock with expiration T and strike X can be priced by:

$$Call = \sum_{i=0}^{n} {n \choose i} \left(q_U^{Public} \right)^i \left(q_D^{Public} \right)^{n-i} Max \left(SU^i D^{n-i} - X, 0 \right)$$

The spreadsheet below shows some sample calculations:

⁶ The assumption of equal access can be weakened, but this does not materially affect our theoretical conclusions.

⁷ This result is so well-known that it really requires no reference, but the interested reader can confirm it in Hull (2010).

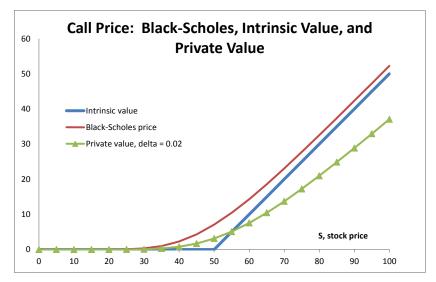
⁸ Abudy and Benninga (2010).

	A	В	C
1	SIMULAT		C AND PRIVATE CALL VALUATIONS
2	Stock price, S	80	
3	Option exercise, X	50	
4	Option maturity, T	0.75	
5			
	Stock price process		
7	μ, mean	15%	
8	σ, standard deviation	35%	
9	r, risk-free	6%	
10	Δt , time interval	0.004	< =1/250
11			
12			< =EXP(mu*delta_t+sigma*SQRT(delta_t))
-	Down		< =EXP(mu*delta_t-sigma*SQRT(delta_t))
14	R	1.0002	< =EXP(rf*delta_t)
15			
16	Public state prices		
17	q _U ^{Public}	0.4862	< =(RDown)/(R_*(Up-Down))
18	q _D ^{Public}	0.5135	< =1/RB17
19			
20	Private state prices		
21	δ, non-diversification effect	0.02	
22		0.4662	< =B17-delta
23	Private QD	0.5335	< =B18+delta
24			
25	Public option price (~Black-Scholes)		< =Binomial_eur_call(Up,Down,R_,B2,B3,ROUND(B4/delta_t,0),0)
26	Private option price	20.9808	< =Binomial_eur_call(Up,Down,R_,B2,B3,ROUND(B4/delta_t,0),delta)
27	Intrinsic	30.0000	< =MAX(B2-B3,0)

The public option price (cell B25) is very close to the Black-Scholes price.⁹ In this particular example, the private option price is 20.98 (cell B26), which is less than the intrinsic value of 30 (cell B27). Thus—in the absence of the opportunity to sell the option—the holder of the option would prefer to exercise early.

When we graph the Black-Scholes price, the intrinsic value, and the private option price, we clearly see that the private price intersects the intrinsic value:

⁹ When $\Delta t \rightarrow 0$, the binomial price using the public state prices converges to the Black-Scholes price. In our example $\Delta t = 0.004$, so that the binomial is a very good approximation to Black-Scholes.

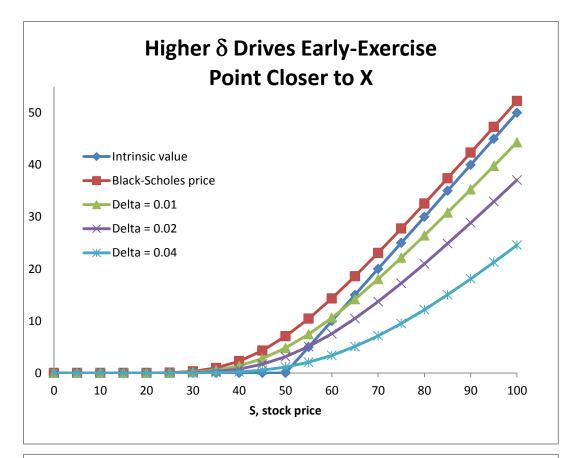


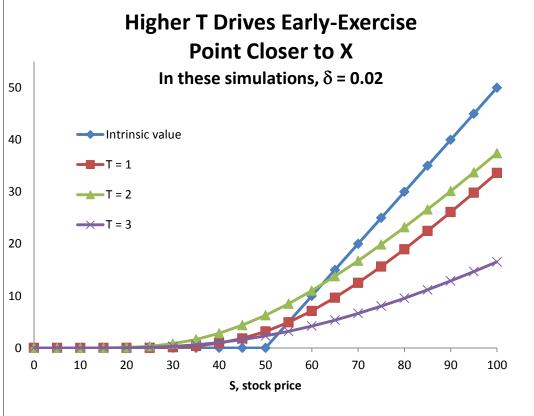
In the above drawing, this happens when S = 55.16. The operative conclusion: If the holder of an ESO is past the vesting period and the stock price > 55.16, then early exercise of the ESO is optimal.

Sensitivity analysis

We can easily do sensitivity analysis on these computations to show the following:

- The crossing point (where intrinsic value = private value) is always greater than S = X.
- The crossing point is a decreasing function of δ. Larger δ implies that the crossing point is closer to S = X.
- The crossing point is a decreasing function of time to option maturity. The larger the option maturity, the closer is the crossing point to S = X.





4. Estimating the public versus the private state prices

In this section we calibrate our model and estimate the non-diversification measure δ using a proprietary data set of employee stock option grants and exercise records. This proprietary data set was obtained from Tamir-Fishman & Co., an Israeli based investment house which offers management services of share-based compensation programs. To respect the anonymity of the data, we identify the companies by a two-digit code and report the results on an aggregate level using two-digit SIC code.

The Tamir-Fishman database is comprised of complete histories of stock option grants, vesting structures, option exercises and cancellation events for employees in both private and public firms. We identify ninety four firms in the database that are either currently public or were public in the past and private firms that were acquired by a public firm and now serve as its subsidiary granted SOPs. These firms are traded in Israel, U.S. and European stock markets.

We process the data according to the following criteria:

- Employees are sometimes forced to exercise their stock options. These forced exercises are usually results of job termination and mergers and acquisitions.¹⁰ We are interested in voluntary exercise records and therefore aim to exclude exercise records that represent forced exercise. As a result, we exclude all exercise records that were made 100 days before or after the employee's job termination date. The 100-day period relates to the common practice that allows employees up to three months to exercise their stock options after they cease working in the company. We exclude 100 days preceding the job termination date to account for the case that the option exercise is part of a plan to cease working in the company.
- The database includes stock options that were granted to service providers who are not employees of the company.¹¹ We are interested in valuing employee stock options, and therefore exclude exercise records of non-employees from our sample.
- In order to price stock options we need to estimate the standard deviation of the underlying stock—a component in setting the value of the state prices as demonstrated in Section 2. We use historical volatility as a proxy of the underlying asset's standard deviation. As a result, we

¹⁰ Forced exercise due to job termination or as a result of mergers and acquisitions is a common practice. In case the company did not force early exercise and the employee exercised his option during 100 days from the job termination, we did not exclude his exercise records from our sample.

¹¹ Companies use this compensation form to compensate service providers without paying cash.

only relate to options that were granted while the underlying security was traded, and exclude exercise records in case the grant date occurred prior to the company's IPO

- An additional requirement with respect to the historical volatility calculation is a minimum of 14 trading days in a month. The reason is straightforward: Stocks with low trading volume underestimate the volatility measure. Therefore, we exclude exercise records in months that this criterion is violated.
- To refrain from bias in the estimation, we exclude exercise records in case a single exercise record resulted in less than 50 shares.
- A stock option with an exercise price of zero is parallel to restricted stock, since the option holder does not pay any amount upon exercise. Since we focus on ESOs, we exclude exercise records with exercise price lower than 0.1.
- We exclude ESO exercise records that were 100 days before the contractual expiration date of the option. As presented on Section 2, the private pricing model results in endogenous early exercise decision. Employees that exercise their options close to expiration are not suitable candidates for examining early exercise patterns and therefore cause to bias in the nondiversification estimation.

The final sample contains 33,294 employee-by-employee exercise records from 65 companies. The sample period of the stock option grants is between 1995 and 2009. The sample period of the exercise records is between 1998 and 2009.

ESO parameters and data sources

The Black-Scholes model and the binomial model require six input parameters: The underlying security price, the option's exercise price, expected standard deviation of the underlying asset, risk free rate, time to expiration and dividend yield.¹² We estimate the ESO value on the grant date and on the exercise date. For each ESO exercise record we match the following estimation:

• <u>Historical volatility</u>: We calculate the historical volatility of the underlying security using the daily continuous compounded return. We require a minimum estimation period of 20 trading

¹² ASC 718 (previously FAS 123(R)) also requires that these input parameters will be included in the valuation model of the equity based compensation.

days from the firm's IPO (subject to 14 trading days in a month restriction). We expand the estimation window to 30 days and then use a rolling window estimation of 30 trading days.¹³ The proxy for the expected volatility is the historical volatility on the calculation date. For example, if we calculate the ESO value on the grant date, then the historical volatility of the underlying security on that date serves as the proxy of the expected volatility in the pricing model.

- <u>Risk free rate</u>: We match a risk free rate according to the currency the company's shares are traded. Hence, if the company's shares are traded in the NASDAQ we use the U.S. T-bill rate.
- <u>Time to expiration</u>: We use the original expiration date of the ESO. Due to insufficient data, ESOs exercise records before 2000 were excluded from the sample. In addition, exercise records of ex-employees in which the original expiration date is identical to the last date of exercise were excluded.¹⁴ We also excluded exercise records of ESO grants of less than four years.
- <u>Dividend yield</u>: We assumed a dividend yield of zero for the sample firms. This assumption fits 80% of the sample firms during (and before) the sample period.
- <u>Vesting period</u>: We assume an average vesting period of three years. This assumption is relevant only to the estimation of ESO at the grant date (the option is already vested when the employee exercises it).

The calculation of the above parameters involved the use of the following data sources: Stock prices were obtained from CRSP, Tel-Aviv stock exchange (TASE) website, Yahoo! Finance and websites of the companies in the sample. Annual risk free rates were obtained from the Federal Reserve Statistical Release website (3 months T-bill) and from websites of central banks in Israel and Europe, such as the Bank of Israel website (MAKAM rates).¹⁵

¹³ We repeat our estimation using an historical volatility calculation of 126 trading days. The results are similar.

¹⁴ The database is managed in a way that the expiration date changes according to the circumstances. For example, if the employee is no longer employed in the company, the expiration date is updated to three months after the job termination date. This update changes the estimation, so we exclude exercise records of grants that lack the original expiration date.

¹⁵ MAKAM is a zero coupon bond issued by the Bank of Israel, parallel to one-year Treasury bill.

Descriptive statistics for the ESO parameters

In this subsection we provide descriptive statistics for the sample companies and the model parameters. The objective is twofold: First, data on ESO grants in scarce. Providing data about practices of this common equity-base compensation form can be useful to policy makers. Second, there is a benefit from the description of the parameters that are being used to estimate the ESO value.

Table 1 describes the industries of the sample companies according to the two-digit firm-level SIC codes. There is considerable heterogeneity in the firm industries in the sample. In addition, a major part of the firms comprising the dataset are new-economy firms related to computers, software, the internet, telecommunications or networking.¹⁶ These firms represent 69.23% of the firms and 73.83% of the exercise records in the sample.

Table 1: Sample Firms De	escription		-
Industry	Two-digit firm-level SIC	Percentage (number of	Percentage (number of
		firms)	employees)
Food And Kindred Products	20	1.54%	0.16%
Paper And Allied Products	26	1.54%	0.73%
Printing, Publishing, And Allied Industries	27	1.54%	0.17%
Chemicals And Allied Products	28	3.08%	0.39%
Industrial And Commercial Machinery And Computer Equipment	35	16.92%	28.71%
Electronic And Other Electrical Equipment And Components,	36	26.15%	38.48%
Except Computer Equipment	50	20.13%	30.40%
Measuring, Analyzing, And Controlling Instruments; Photographic,	38	7.69%	7.22%
Medical And Optical Goods; Watches And Clocks	00	1.00 %	1.2270
Communications	48	7.69%	7.73%
Wholesale Trade-durable Goods	50	1.54%	0.20%
Depository Institutions	60	1.54%	2.09%
Business Services	73	26.15%	6.64%
Engineering, Accounting, Research, Management, And Related Services	87	4.62%	7.48%

The summary statistics in Tables 2 and 3 present the original time to expiration of the options (in years) and on the remaining time to expiration of the options at the exercise date (in years), respectively. The remaining time until expiration of the option is used to estimate the value of the nondiversification measure δ on the exercise date and the original time to expiration of the option is used to value the option on the grant date. Table 2 presents a quite homogeneous picture: The average contractual option life ranges between eight to ten years, with some options grants for 16 years. Combined with the data of Table 3, it indicates that on average the ESOs in the sample are exercised when there are nearly two-thirds to half of the option term remaining. These findings are consistent

¹⁶ New economy firms defined as companies with primary SIC codes 3570, 3571, 3572, 3576, 3577, 3661, 3674, 4812, 4813, 5045, 5961, 7370, 7371, 7372 and 7373 (See Hall and Murphy 2003). As mentioned, we identify the companies using 2-digit SIC codes.

with the findings of previous studies such as Huddart and Lang (1996) and Carpenter, Stanton and Wallace (2009). The sectors that deviate from this early exercise pattern are the food and kindred products and the paper and allied products (SIC codes 20 and 26, respectively).

Table 2: Time to maturity (in years) of the option								
Industry	Average	SD	Max	Min	1st quartile	4th quartile		
Full Sample	8.087	1.918	16.008	4.003	6.005	10.005		
Food And Kindred Products	6.283	0.931	8.005	4.268	5.851	6.923		
Paper And Allied Products	5.225	0.839	9.005	4.003	5.003	5.003		
Printing, Publishing, And Allied Industries	10.008	0.001	10.008	10.005	10.008	10.008		
Chemicals And Allied Products	10.023	0.039	10.181	10.005	10.005	10.008		
Industrial And Commercial Machinery And Computer Equipment	7.162	1.571	10.507	4.123	6.003	8.003		
Electronic And Other Electrical Equipment And Components,	9.091	1.511	16.008	4.003	7.164	10.008		
Except Computer Equipment	9.091	1.511	10.000	4.003	7.104	10.008		
Measuring, Analyzing, And Controlling Instruments; Photographic,	5.785	1.628	10.008	4.003	5.000	5.003		
Medical And Optical Goods; Watches And Clocks	5.765	1.020	10.008	4.003	5.000	5.003		
Communications	9.751	0.572	10.008	5.849	10.005	10.005		
Wholesale Trade-durable Goods	9.312	1.270	10.433	6.499	9.501	10.005		
Depository Institutions	5.741	0.761	7.247	4.003	6.000	6.000		
Business Services	9.032	1.844	10.008	4.003	9.871	10.008		
Engineering, Accounting, Research, Management, And Related	6.938	0.679	10.008	4.044	7.003	7.005		
Services	0.930	0.079	10.008	4.044	7.003	7.005		
Entire sample, employees	8.066	1.921	16.008	4.003	6.005	10.005		
Entire sample, executives (Directors and Officers)	8.684	1.728	10.079	4.003	7.005	10.008		
Entire sample, exercise (cash)	8.941	1.809	16.008	4.003	7.045	10.008		
Entire sample, SDS (same day sale)	8.080	1.917	16.008	4.003	6.005	10.005		
This table reports the time to maturity of the option grants at the gro	ant date. The tin	ne to maturity is	measured as th	ne numbe	er of years bet	ween the		
grant date and the expiration date of the option grant. The summar	ry statistics are o	computed over	all the exercise	records	in the sample	period. The		
summary statistics by the two-digit firm-level SIC categories as repo	rted in CRSP.							

Industry	Average	SD	Max	Min	1st quartile	4th quartile
Full Sample	4.669	2.334	9.978	0.274	2.871	6.564
Food And Kindred Products	1.868	0.770	2.975	0.529	1.104	2.555
Paper And Allied Products	1.527	0.768	4.003	0.288	0.852	1.979
Printing, Publishing, And Allied Industries	7.068	0.735	8.553	5.441	6.679	7.512
Chemicals And Allied Products	6.949	1.467	9.373	0.630	6.370	7.904
Industrial And Commercial Machinery And Computer Equipment	3.831	2.036	9.318	0.274	2.373	4.981
Electronic And Other Electrical Equipment And Components, Except Computer Equipment	5.417	2.129	9.948	0.274	4.025	7.167
Measuring, Analyzing, And Controlling Instruments; Photographic, Medical And Optical Goods; Watches And Clocks	2.417	1.955	9.781	0.274	0.923	2.836
Communications	6.679	1.638	9.948	0.282	5.841	7.879
Wholesale Trade-durable Goods	8.493	1.093	9.663	5.975	8.600	8.992
Depository Institutions	3.101	1.317	6.197	0.395	1.962	4.196
Business Services	5.973	2.194	9.978	0.282	4.460	7.674
Engineering, Accounting, Research, Management, And Related Services	3.506	1.439	9.266	0.282	2.577	4.490
Entire sample, employees	4.630	2.333	9.978	0.274	2.830	6.460
Entire sample, executives (Directors and Officers)	5.749	2.115	9.748	0.477	4.013	7.504
Entire sample, exercise (cash)	5.238	2.399	9.660	0.282	3.586	7.274
Entire sample, SDS (same day sale)	4.664	2.333	9.978	0.274	2.866	6.554

digit firm-level SIC categories ass reported by CRSP.

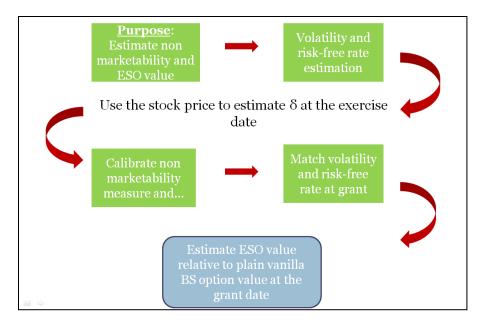
Table 4 reports the summary statistics of the stock price to the exercise price ratio in the sample. There is a difference in the ratios both across and within sectors. The highest ratios reflect runups in the stock market during our sample period. Specifically, these ratios stem from market runups during the end of the 1990s and the beginning of 2000. In general, the option exercise patterns present

evidence on the persistence of early exercise behavior along with considerable heterogeneity both within and across sectors. These findings are consistent with the findings of previous studies such as Carpenter, Stanton and Wallace (2009) and Bettis, Bigjak and Lemmon (2005).

Food And Kindred Products2.6030.9033.9721.3581.6133.339Paper And Allied Products2.5120.9625.5901.2571.8682.562Printing, Publishing, And Allied Industries2.9640.6714.3391.6542.6193.56Chemicals And Allied Products1.9580.6005.1521.0121.4852.33Industrial And Commercial Machinery And Computer Equipment3.3393.31439.7671.0061.5514.05Electronic And Other Electrical Equipment And Components, Except Computer Equipment2.8713.31137.7581.0011.2813.41Measuring, Analyzing, And Controlling Instruments; Photographic, Medical And Optical Goods; Watches And Clocks2.8932.57728.9801.0091.5482.52Wholesale Trade-durable Goods2.1590.8945.5311.0931.7442.16Depository Institutions1.5620.1841.8781.0191.4401.66Business Services3.9264.47626.1581.0011.4714.24Endineering, Accounting, Research, Management, And Related Services2.1280.8228.2811.0281.5802.32Enfire sample, executives (Directors and Officers)3.3422.30125.0001.0331.7574.17Enfire sample, executives (Directors and Officers)3.3422.30125.0001.0331.7574.17Enfire sample, exercise (cash)4.3165.77433.1631.002<	Industry	Average	SD	Max	Min	1st quartile	4th quartile
Paper And Allied Products 2.512 0.962 5.590 1.257 1.868 2.562 Printing, Publishing, And Allied Industries 2.964 0.671 4.339 1.654 2.619 3.562 Chemicals And Allied Products 1.958 0.600 5.152 1.012 1.485 2.351 Industrial And Commercial Machinery And Computer Equipment 3.339 3.314 39.767 1.006 1.551 4.095 Electronic And Other Electrical Equipment And Components, Except Computer Equipment 2.871 3.311 37.758 1.001 1.281 3.41 Measuring, Analyzing, And Controlling Instruments; Photographic, Medical And Optical Goods; Watches And Clocks 1.892 1.250 30.415 1.010 1.368 1.86 Communications 2.393 2.577 28.980 1.009 1.548 2.57 Wholesale Trade-durable Goods 2.159 0.894 5.531 1.093 1.744 2.16 Business Services 3.926 4.476 26.158 1.001 1.471 4.24 Engineering, Accounting, Research, Management, And Related Services 2.128 0.822 8.281 1.028	Full Sample	2.877	3.114	39.767	1.001	1.381	3.278
Printing, Publishing, And Allied Industries2.9640.6714.3391.6542.6193.56Chemicals And Allied Products1.9580.6005.1521.0121.4852.33Industrial And Commercial Machinery And Computer Equipment3.3393.31439.7671.0061.5514.09Electronic And Other Electrical Equipment And Components, Except Computer Equipment2.8713.31137.7581.0011.2813.41Measuring, Analyzing, And Controlling Instruments; Photographic, Medical And Optical Goods; Watches And Clocks1.8921.25030.4151.0101.3681.86Communications2.3932.57728.9801.0091.5482.55Wholesale Trade-durable Goods2.1590.8945.5311.0031.7442.15Business Services3.9264.47626.1581.0011.4714.246Engineering, Accounting, Research, Management, And Related Services2.1280.8228.2811.0281.5802.352Enfire sample, employees2.8603.13839.7671.0011.3713.2323.3422.30125.0001.0331.7574.17Enfire sample, exercise (cash)4.3165.77433.1631.0221.4123.888	Food And Kindred Products	2.603	0.903	3.972	1.358	1.613	3.393
Chemicals And Allied Products 1.958 0.600 5.152 1.012 1.485 2.33 Industrial And Commercial Machinery And Computer Equipment 3.339 3.314 39.767 1.006 1.551 4.09 Electronic And Other Electrical Equipment And Components, Except Computer Equipment 2.871 3.311 37.758 1.001 1.281 3.41 Measuring, Analyzing, And Controlling Instruments; Photographic, Medical And Optical Goods; Watches And Clocks 1.892 1.250 30.415 1.010 1.368 1.86 Communications 2.393 2.577 28.980 1.009 1.548 2.55 Wholesale Trade-durable Goods 2.159 0.894 5.531 1.009 1.440 1.68 Business Services 3.926 4.476 26.158 1.001 1.471 4.24 Engineering, Accounting, Research, Management, And Related Services 2.128 0.822 8.281 1.028 1.580 2.32 Enfire sample, employees 2.860 3.138 39.767 1.001 1.371 3.23 Enfire sample, execu	Paper And Allied Products	2.512	0.962	5.590	1.257	1.868	2.563
Industrial And Commercial Machinery And Computer Equipment 3.339 3.314 39.767 1.006 1.551 4.005 Electronic And Other Electrical Equipment And Components, Except Computer Equipment 2.871 3.311 37.758 1.001 1.281 3.41 Measuring, Analyzing, And Controlling Instruments; Photographic, Medical And Optical Goods; Watches And Clocks 1.892 1.250 30.415 1.010 1.368 1.862 Communications 2.393 2.577 28.980 1.009 1.548 2.552 Wholesale Trade-durable Goods 2.159 0.894 5.531 1.001 1.440 1.668 Business Services 3.926 4.476 26.158 1.001 1.471 4.246 Engineering, Accounting, Research, Management, And Related Services 2.128 0.822 8.281 1.028 1.580 2.365 Enfire sample, employees 2.860 3.138 39.767 1.001 1.371 3.225 Enfire sample, executives (Directors and Officers) 3.342 2.301 25.000 1.033 1.757 4.175 Enfire sample, exercise (cash) 4.316 5.774 33.163 </td <td>Printing, Publishing, And Allied Industries</td> <td>2.964</td> <td>0.671</td> <td>4.339</td> <td>1.654</td> <td>2.619</td> <td>3.500</td>	Printing, Publishing, And Allied Industries	2.964	0.671	4.339	1.654	2.619	3.500
Electronic And Other Electrical Equipment And Components, Except Computer Equipment 2.871 3.311 37.758 1.001 1.281 3.41 Measuring, Analyzing, And Controlling Instruments; Photographic, Medical And Optical Goods; Watches And Clocks 1.892 1.250 30.415 1.010 1.368 1.862 Communications 2.393 2.577 28.980 1.009 1.548 2.552 Wholesale Trade-durable Goods 2.159 0.894 5.531 1.010 1.440 2.159 Depository Institutions 1.562 0.184 1.878 1.011 1.440 1.663 Business Services 3.926 4.476 26.158 1.001 1.411 4.244 Engineering, Accounting, Research, Management, And Related Services 2.128 0.822 8.281 1.028 1.580 2.393 Enfire sample, employees 2.860 3.138 39.767 1.001 1.371 3.223 Enfire sample, executives (Directors and Officers) 3.342 2.301 25.000 1.033 1.757 4.17 Enfire sample, exercise (cash) 4.316 5.774 33.163 1.022 1.	Chemicals And Allied Products	1.958	0.600	5.152	1.012	1.485	2.359
Except Computer Equipment2.8713.31137.7581.0011.2813.41Measuring, Analyzing, And Controlling Instruments; Photographic, Medical And Optical Goods; Watches And Clocks1.8921.25030.4151.0101.3681.862Communications2.3932.57728.9801.0091.5482.522Wholesale Irade-durable Goods2.1590.8945.5311.0931.7442.162Depository Institutions1.5620.1841.8781.0101.4401.663Business Services3.9264.47626.1581.0011.4714.242Engineering, Accounting, Research, Management, And Related Services2.1280.8228.2811.0281.5802.363Enfire sample, employees2.8603.13839.7671.0011.3713.223Enfire sample, executives (Directors and Officers)3.3422.30125.0001.0331.7574.175Enfire sample, exercise (cash)4.3165.77433.1631.0221.4123.884	Industrial And Commercial Machinery And Computer Equipment	3.339	3.314	39.767	1.006	1.551	4.091
Medical And Optical Goods; Watches And Clocks 1.892 1.250 30.415 1.010 1.368 1.892 Communications 2.393 2.577 28.980 1.009 1.548 2.552 Wholesale Trade-durable Goods 2.159 0.894 5.531 1.093 1.744 2.159 Depository Institutions 1.562 0.184 1.878 1.010 1.440 1.662 Business Services 3.926 4.476 26.158 1.001 1.440 1.662 Engineering, Accounting, Research, Management, And Related Services 2.128 0.822 8.281 1.028 1.580 2.393 Entire sample, employees 2.860 3.138 39.767 1.001 1.371 3.223 Entire sample, executives (Directors and Officers) 3.342 2.301 25.000 1.033 1.757 4.175 Entire sample, exercise (cash) 4.316 5.774 33.163 1.022 1.412 3.883		2.871	3.311	37.758	1.001	1.281	3.414
Wholesale Trade-durable Goods 2.159 0.894 5.531 1.093 1.744 2.159 Depository Institutions 1.562 0.184 1.878 1.019 1.440 1.662 Business Services 3.926 4.476 26.158 1.001 1.471 4.242 Engineering, Accounting, Research, Management, And Related Services 2.128 0.822 8.281 1.028 1.580 2.352 Enfire sample, employees 2.860 3.138 39.767 1.001 1.371 3.222 Enfire sample, executives (Directors and Officers) 3.342 2.301 25.000 1.033 1.757 4.172 Enfire sample, exercise (cash) 4.316 5.774 33.163 1.022 1.412 3.883		1.892	1.250	30.415	1.010	1.368	1.869
Depository Institutions 1.562 0.184 1.878 1.019 1.440 1.66 Business Services 3.926 4.476 26.158 1.001 1.471 4.24 Engineering, Accounting, Research, Management, And Related Services 2.128 0.822 8.281 1.028 1.580 2.38 Enfire sample, employees 2.860 3.138 39.767 1.001 1.371 3.23 Enfire sample, executives (Directors and Officers) 3.342 2.301 25.000 1.033 1.757 4.17 Enfire sample, exercise (cash) 4.316 5.774 33.163 1.022 1.412 3.88	Communications	2.393	2.577	28.980	1.009	1.548	2.525
Business Services 3.926 4.476 26.158 1.001 1.471 4.24 Engineering, Accounting, Research, Management, And Related Services 2.128 0.822 8.281 1.028 1.580 2.38 Enfire sample, employees 2.860 3.138 39.767 1.001 1.371 3.22 Enfire sample, executives (Directors and Officers) 3.342 2.301 25.000 1.033 1.757 4.17 Enfire sample, exercise (cash) 4.316 5.774 33.163 1.022 1.412 3.88	Wholesale Trade-durable Goods	2.159	0.894	5.531	1.093	1.744	2.196
Engineering, Accounting, Research, Management, And Related 2.128 0.822 8.281 1.028 1.580 2.38 Services 2.860 3.138 39.767 1.001 1.371 3.23 Enfire sample, employees 2.860 3.138 39.767 1.001 1.371 3.23 Enfire sample, executives (Directors and Officers) 3.342 2.301 25.000 1.033 1.757 4.17 Enfire sample, exercise (cash) 4.316 5.774 33.163 1.022 1.412 3.88	Depository Institutions	1.562	0.184	1.878	1.019	1.440	1.695
Services 2.128 0.822 8.281 1.028 1.880 2.38 Enfire sample, employees 2.860 3.138 39.767 1.001 1.371 3.23 Enfire sample, executives (Directors and Officers) 3.342 2.301 25.000 1.033 1.757 4.17 Enfire sample, exercise (cash) 4.316 5.774 33.163 1.022 1.412 3.88	Business Services	3.926	4.476	26.158	1.001	1.471	4.242
Entire sample, executives (Directors and Officers) 3.342 2.301 25.000 1.033 1.757 4.17 Entire sample, exercise (cash) 4.316 5.774 33.163 1.022 1.412 3.88		2.128	0.822	8.281	1.028	1.580	2.395
Enfire sample, exercise (cash) 4.316 5.774 33.163 1.022 1.412 3.88	Enfire sample, employees	2.860	3.138	39.767	1.001	1.371	3.236
	Entire sample, executives (Directors and Officers)	3.342	2.301	25.000	1.033	1.757	4.176
	Entire sample, exercise (cash)	4.316	5.774	33.163	1.022	1.412	3.883
Entire sample, SDS (same day sale) 2.865 3.080 39.767 1.001 1.381 3.27	Entire sample, SDS (same day sale)	2.865	3.080	39.767	1.001	1.381	3.273

Estimation of the non-diversification measure δ and the ESO value

Our purpose is to estimate the value of the ESO on the grant date. We employ the following procedure: In the first step we estimate the non-diversification measure δ on the exercise date. In this estimation procedure we use the stock price on the exercise date, along with the additional option parameters such as the underlying security volatility. The second step occurs on the ESO's grant date. We use the estimated non-diversification measure (from the first step) and calibrate it into the private pricing model. The result is as estimation of the ESO value. Since the second step is made on the grant date, we use the ESO's characters at this stage to the ESO value (The only character of the model which is not time-adjusted is the non-diversification measure that we estimated in the first step, on the ESO's exercise date) using the private pricing model. Then, we calculate the value of a plain vanilla Black-Scholes option on the grant date (using the ESO characters), and divide the private option value by the Black-Scholes option value. The outcome is a measure of the value of the ESO to the employee on the grant date. The figure below summarizes the estimation procedure.



The non-diversification measure δ is a specific parameter of the private pricing model and as far as we know, it is the first attempt to estimate it. Applying this model requires data on nontradable securities and financial instruments, and such information is usually non-public information. In the case of ESOs, for example, firm disclose only necessary information required by regulators. Such information relates mainly to executives, and not to non-executive employees. As a result, multinational comparison of δ is not-available.

Table 5 presents the estimation results of the non-diversification measure δ . This estimation is made on the option's (early) exercise date, using the stock price on that date, along with the specific characters of each company, such as the risk free rate, volatility, dividend yield and exit rate.¹⁷ In addition to industry partitions, we also calculate an average data for non-executive employees relative to executives and to exercise records of employees that continue to hold the stock after the option's exercise relative to exercise records of employees which sell the stock immediately after the option exercise (cashless exercise). The average non-diversification measure δ in the entire sample equals 0.025, with a similar tendency within the SIC sectors except for the food and kindred products and the paper and allied products (SIC codes 20 and 26, respectively), which have smaller δ values. It means that, ceteris paribus, employees in these industries are more diversified than employees in other industries in the sample. This finding fits the common practice of a higher tendency to grant options in 'new-economy' firms. In addition, according to Table 5 results executives have a lower non-diversification measure relative to non-executive employees. It means that, ceteris paribus, a greater

¹⁷ We do not use vesting here because if the stock option can be exercised it means that it is after vesting.

fraction of non-executive employees' wealth is, on average, in assets that cause them to be undiversified comparing to executives. A possible explanation is that executives are more aware to the benefits of diversification (for example, Guiso and Jappelli (2008) find strong correlation between measures of financial literacy with the degree of portfolio diversification). It also imply that executives tend to exercise their stock options later (or closer to expiration) than rank and file employees.

Table 5: The non-marketability estimation using the stock price at the exercise date									
Industry	Average	SD	Max	Min	1st quartile	4th quartile			
Full Sample	0.025	0.036	0.474	0.000	0.005	0.030			
Food And Kindred Products	0.009	0.007	0.027	0.002	0.004	0.014			
Paper And Allied Products	0.010	0.006	0.035	0.003	0.007	0.011			
Printing, Publishing, And Allied Industries	0.008	0.004	0.019	0.004	0.005	0.009			
Chemicals And Allied Products	0.021	0.031	0.285	0.001	0.007	0.025			
Industrial And Commercial Machinery And Computer Equipment	0.020	0.031	0.414	0.000	0.003	0.025			
Electronic And Other Electrical Equipment And Components,	0.032	0.044	0.469	0.000	0.006	0.039			
Except Computer Equipment	0.032	0.044	0.409	0.000	0.008	0.039			
Measuring, Analyzing, And Controlling Instruments; Photographic,	0.023	0.026	0.319	0.000	0.010	0.025			
Medical And Optical Goods; Watches And Clocks	0.023	0.020	0.319	0.000	0.010	0.025			
Communications	0.023	0.029	0.353	0.000	0.008	0.025			
Wholesale Trade-durable Goods	0.030	0.028	0.160	0.004	0.016	0.028			
Depository Institutions	0.026	0.027	0.299	0.007	0.015	0.026			
Business Services	0.023	0.033	0.474	0.000	0.005	0.029			
Engineering, Accounting, Research, Management, And Related	0.018	0.021	0.291	0.000	0.008	0.021			
Services	0.018	0.021	0.291	0.000	0.008	0.021			
Entire sample, employees	0.026	0.036	0.474	0.000	0.005	0.031			
Entire sample, executives (Directors and Officers)	0.016	0.021	0.328	0.000	0.004	0.022			
Entire sample, exercise (cash)	0.027	0.042	0.328	0.000	0.004	0.032			
Enfire sample, SDS (same day sale) 0.025 0.036 0.474 0.000 0.005 0.030									
This table reports the non-marketability estimation at the exercise do	ate. We value th	ne non-marketo	bility using the	spesific c	haracthers of	each			
exercise record. Time to maturity is measured as the number of yea	rs between the	exercise date of	and the origina	expiratio	n date of the	option grant.			
Annual risk free rate is adjusted according to the share's currency.	olatility is estim	ated by historic	al volatility of t	ne share.	The summary s	statistics are			
computed over all the exercise records in the sample period and g	rouped using tv	vo-diait firm-lev	el SIC categori	es as repo	orted in CRSP.				

Table 6 presents the estimation results. These estimations calibrate the non-diversification measure from Table 5 with the annual risk free rate, historical volatility, contractual option life, vesting period and dividend yield—all on the grant date. All this data is used to calculate both the ESO private value and the plain vanilla Black-Scholes value on the grant date.

Table 6: ESO private value relaitive to Black–Scholes value (in percentage) at the grant date								
Industry	Average	SD	Max	Min	1st quartile	4th quartile		
Full Sample	48.23%	29.62%	99.97%	0.00%	22.01%	74.24%		
Food And Kindred Products	69.06%	16.17%	89.36%	32.05%	57.79%	82.24%		
Paper And Allied Products	68.32%	13.21%	88.35%	25.40%	62.34%	76.02%		
Printing, Publishing, And Allied Industries	65.30%	9.82%	76.42%	37.53%	60.05%	73.31%		
Chemicals And Allied Products	50.35%	24.21%	93.75%	0.00%	31.24%	70.02%		
Industrial And Commercial Machinery And Computer Equipment	57.97%	30.62%	99.97%	0.00%	29.92%	85.37%		
Electronic And Other Electrical Equipment And Components, Except Computer Equipment	41.21%	30.37%	99.80%	0.00%	13.27%	70.14%		
Measuring, Analyzing, And Controlling Instruments; Photographic, Medical And Optical Goods; Watches And Clocks	47.15%	23.59%	98.87%	0.00%	32.45%	60.94%		
Communications	43.73%	24.55%	99.17%	0.00%	28.47%	62.45%		
Wholesale Trade-durable Goods	30.92%	18.55%	74.89%	0.00%	21.45%	39.14%		
Depository Institutions	44.78%	17.30%	73.96%	0.00%	36.69%	56.42%		
Business Services	48.47%	28.91%	99.46%	0.00%	26.03%	74.18%		
Engineering, Accounting, Research, Management, And Related Services	50.92%	24.96%	97.57%	0.00%	33.22%	68.91%		
Entire sample, employees	47.98%	29.68%	99.97%	0.00%	21.68%	74.05%		
Entire sample, executives (Directors and Officers)	55.07%	27.00%	97.57%	0.00%	32.96%	78.73%		
Entire sample, exercise (cash)	51.28%	32.34%	99.77%	0.00%	22.11%	80.45%		
Entire sample, SDS (same day sale)	48.20%	29.59%	99.97%	0.00%	22.00%	74.20%		
This table reports the value of the ESO using the private pricing mod date. The non-marketability measure was estimatied at the exercise of years between the grant date and the original expiration date of currency. Volatility is estimated by historical volatility of the stock. Th	date and calib the option gro	, prated into the r nt. Annual risk fr	nodel. Time to r ee rate is adjus	maturity is ted acco	measured as ording to the s	the number hare's		
period, and grouped using two-digit firm-level SIC categories as rep								

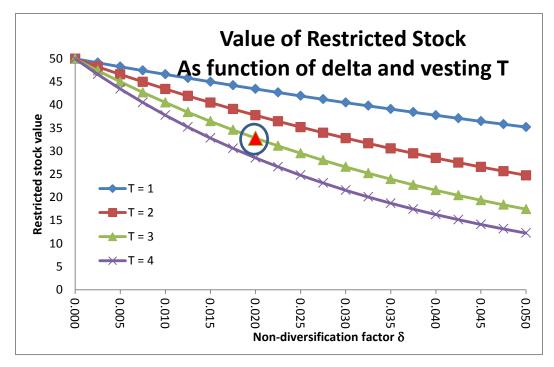
According to our estimation, the private ESO value is, on average, about 50% relative to a plainvanilla BS value. In the food and kindred products and the paper and allied products (SIC codes 20 and 26, respectively) industries the value is higher—around 65%. Note that the first and fourth quintiles of these industries are also quite high. This finding results from a lower non-diversification measure and from smaller volatilities in these industries. In addition, the lower non-diversification measure of executives results in their higher estimation of ESO value.

Table 6 findings are consistent with predictions of other academic papers regarding ESO value. For example Meulbroek (2001) predicts that in new economy firms (with exhibit higher stock volatility), an undiversified manager would assign lower value to his stock options relative to an un-diversified manager from less volatile industries. Our findings are also consistent with the findings of Ikaheimo et al. (2006), which use the prices of tradable executive stock options, traded at the Helsinki stock exchange after the options are vested (which means these are transferable stock options). By analyzing 27,808 trades, Ikaheimo et al. (2006) show major underpricing of the ESO which can reach over 50% discount relative to Black-Scholes value. Since Ikaheimo et al. (2006) examine tradable stock options, the nonmarketability associated with these options should be less comparing to the standard case of untradeable stock options (which is the case of the stock options in Tamir-Fishman sample). It implies that the untradeable stock options the discount should be higher than the one found by Ikaheimo et al. (2006). In addition, the results ascribe higher option values to executives compared to ESO values to non-executive employees. Overall, these results point out on a relative high discount on equity based compensation.

5. Valuation of restricted stocks units

Restricted stocks are additional form of equity based compensation. In this compensation form, the employee is granted with either right to receive stocks once the vesting requirements are met or with stocks which are restricted until the vesting requirements are met. These compensation forms are called restricted stocks units (RSU) and restricted stock (RS), respectively, with RSU being the more common between the two. The key difference is that since RSU programs deliver the stocks to the employee only after the vesting period while RS programs deliver the (restricted) stocks at the grant date. Thus, RSU holders have no voting rights and usually are not entitled to receive dividend or dividend equivalents.

In this paper we use the private pricing model to value RSU. Since RSUs are not tradable only during the vesting period, we use private state prices with exogenous exit rate during the vesting period, (in which the stocks are non-tradable and the employee is subject to forfeit of the stocks upon job termination). After the vesting period, when the stock is tradable and unrestricted, we use public state prices without any other restrictions. Putting this differently, we basically discount the value of the stock on the vesting date and consider the non-marketability and forfeit restrictions while discounting. The following figure presents the value of δ .



The circled point shows that a restricted stock with a 3-year maturity and a non-diversification factor of δ = 0.02 is worth less than 70% of the value of a non-restricted stock.

6. Summary

The valuation of employee stock options (ESOs) and restricted stock units (RSUs) is problematic for both accountants and finance professionals. The valuation models currently make us of standard valuations based either on Black-Scholes or on lattice approach which have been adjusted to compensate for the special features of typical ESOs. The basis of these valuation models remains, however, the assumption of perfect markets, full employee diversification, and hedgability of the option grants.

In this paper we develop and calibrate a simple model that can account for non-diversification. This non-diversification framework allows us to price ESOs and RSUs. In the case of ESOs, our model provides an endogenous explanation of early ESO exercise that has previously been absent in the literature. Furthermore, the model has empirical content: We show—using a large, proprietary, data base of ESOs—that the model's non-diversification measure can be measured and applied directly to valuations.

References

- Abudy, M., Benninga, S., 2010. Non-Marketability and the Value of Equity Based Compensation. Working paper, Tel-Aviv University.
- Benninga, S., *Financial Modeling*, 3rd edition, MIT Press, 2008.
- Benninga, S., Helmantel, M., Sarig, O., 2005. The Timing of Initial Public Offering. *Journal of Financial Economics* 75, 115-132.
- Bettis, C., Bigjak, J., Lemmon, M., 2005. Exercise Behavior, Valuation, and the Incentive Effects of Employee Stock Options. *Journal of Financial Economics* 76, 445-470.
- Black, F., Scholes, M., 1973. The Pricing of Options and Corporate Liabilities. Journal of Political Economy 81(3), 637-654.
- Carpenter, J., Stanton, R., Wallace, N., 2009. Estimation of Employee Stock Option Exercise Rates and Firm Costs. Available at http://hdl.handle.net/2451/27844.
- Chance, D., 2004. Expensing Executive Stock Options: Sorting Out the Issues. Available at SSRN: http://ssrn.com/abstract=590324.
- Cox, J., Ross, S., Rubinstein, M., 1979. Option Pricing: A Simplified Approach. *Journal of Financial Economics* 7, 229-264.
- Cvitanić, J., Wiener, Z., Zapatero, F., 2007. Analytic Pricing of Employee Stock Options, *Review of Financial Studies* 21, 683-724.
- Finnerty, D. J., 2005. Extending the Black-Scholes-Merton Model to Value Employee Stock Options. Journal of Applied Finance 15(2), 25.
- Hall, J., Murphy, J., 2002. Stock Options for Undiversified Executives. *Journal of Accounting and Economics* 33(1), 3-42.
- Hall, J., Murphy, J., 2003. The Trouble with Stock Options. Journal of Economic Perspectives 17, 49-70.
- Huddart, S., Lang, M., 1996. Employee Stock Option Exercises: An Empirical Analysis. *Journal of* Accounting and Economics 21 (1996), 5-43.
- Huddart, S., Lang, M., 2003. Information Distribution within Firms: Evidence from Stock Option exercises. *Journal of Accounting and Economics* 34, 3-31.
- Hull, J., 2010. Options, Futures, and Other Derivatives. 7th Edition, Prentice-Hall.
- Hull, J., White, A., 2004. How to Value Employee Stock Options, *Financial Analysts Journal* 60, 114-119.
- Ikaheimo, S., Kousa, N., Puttonen, V., 2006. 'The True and Fair Value' of Executive Stock Option Valuation. *European Accounting Review* 15(3), 351-366.

- Meulbroek, L., 2001. The Efficiency of Equity-Link Compensation: Understanding the Full Cost of Awarding Executive Stock Options. *Financial Management* 30(2), 5-30.
- Rubinstein, M., 1995. On the Accounting Valuation of Employee Stock Options. *The Journal of Derivatives* 3, 8-24.